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PAPER

Finite Difference Approximation for Valuation of Option Prices with Dividend Payments of the Underlying Assets

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The development and the expansion of financial derivatives can be considered as the most significant events in finance during the past decade. The main purposes of the derivatives are hedging or providing risk reduction, arbitrage, and speculation. In the 1970s, Black, Scholes, and Merton developed the Black-Scholes partial differential equation considering the no-arbitrage principle for pricing financial derivatives. However, the efficient computation of prices and hedges for derivative products is a major concern for financial institutions since various assumptions and simplifications have to be made in order to obtain an analytical solution of the Black-Scholes equation. Hence, the resulting analytical solution does not reflect the reality. The remedy consists of discretization of the Black-Scholes equations using some numerical technique in order to obtain an approximate solution. Throughout this work, we present some Finite Difference Methods for solving the Black-Scholes model with dividend payments and discuss their convergence properties.

References:

- [1] Bernnan, M.J. & Schwartz, E.S., (1976). The Valuation of American Put Options. *The Journal of Finance*, Vol.32 (2):449-462
- [2] Bernnan, M.J. & Schwartz, E.S., (1978). Finite Difference Methods and Jump Process Arising in the Pricing of Contingent Claims: A Synthesis. *The Journal of Financial and Quantitative Analysis*, Vol. 13(3): 461-474
- [3] Black, F. & Scholes ,M., (1973). The Pricing of Options and Corporate Liabilities. *Journal of Political Economy*, Vol. 81 (3):637 - 654.
- [4] Hull J. & Basu, S.(2010). Options, Futures and Other Derivatives. Pearson Education Inc, Seventh Edition, New Jersey.
- [5] Hull J. & White A. (1990). Valuing Derivative Securities using the Explicit Finite Difference Method. *Journal of Financial and Quantitative Analysis*. Vol. 25(1), 87-100.
- [6] Premarathna L.P.N.D & Karunathilaka N.G.A., (2011), The valuation of options using Finite Difference Methods. Annual Research Symposium, University of Kelaniya.
- [7] Premarathna L.P.N.D,(2012), The Valuation of Options using Finite Difference Methods & Finite Element Methods”, Master Degree Thesis for the fulfillment of the Master of Financial Mathematics, University of Moratuwa, Sri Lanka